

VERIFICA A FLESSIONE, I STADIO

$$\varepsilon = \varepsilon_G + \chi_x X + \chi_y Y$$

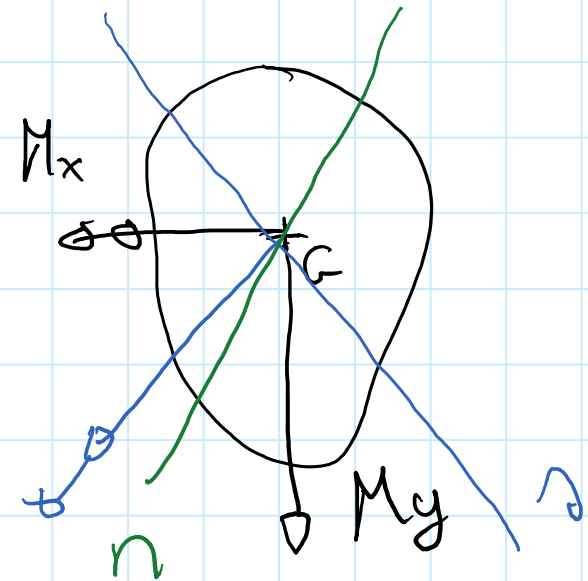
$$\varepsilon_G = \frac{N}{E_c A_{ci}} \quad ; \quad \chi_x = - \frac{M_y}{E_c I_y} \quad \chi_y = \frac{M_x}{E_c I_x}$$

$$N = 0 \quad \rightarrow \quad \varepsilon_G = 0 \quad \Rightarrow$$

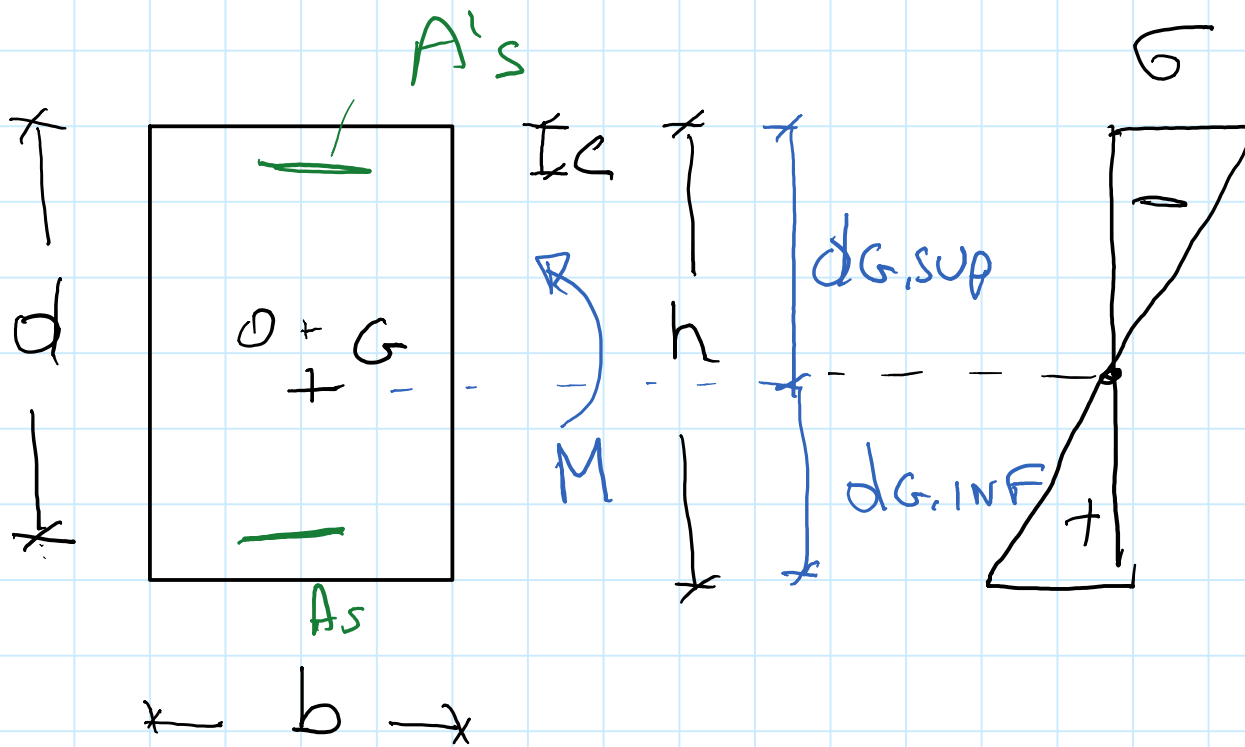
ASSE NEUTRO
PASSA PER G
(SEZ. OMOGENE.)

$$\sigma = - \frac{M_y}{I_y} x + \frac{M_x}{I_x} y$$

λ = ASSE DI SOLLECITAZIONE M
 n = ASSE NEUTRO



FLESSIONE RETTA



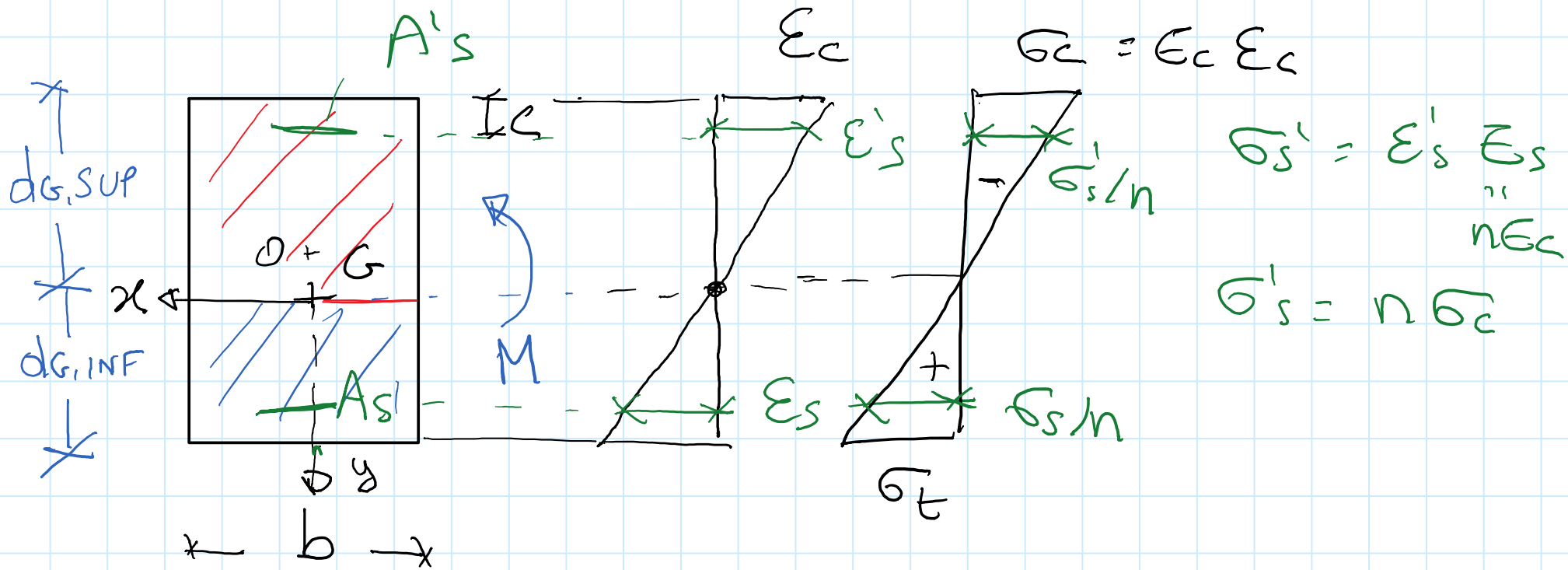
A_s ARMATURA TESA
 $A's$ " COMPRESSA
 C COPRIFERRO
 d ALTEZZA UTILE

$$d_{G,sup} = \frac{S_{sup}}{A}$$

$$S_{sup} = bh \cdot \frac{h}{2} + nA's c + nA_s d$$

$$A = bh + nA's + nA_s$$

$$n = \frac{E_s}{E_c}$$



$$\sigma_t = \frac{M}{I_x} \cdot dG,INF$$

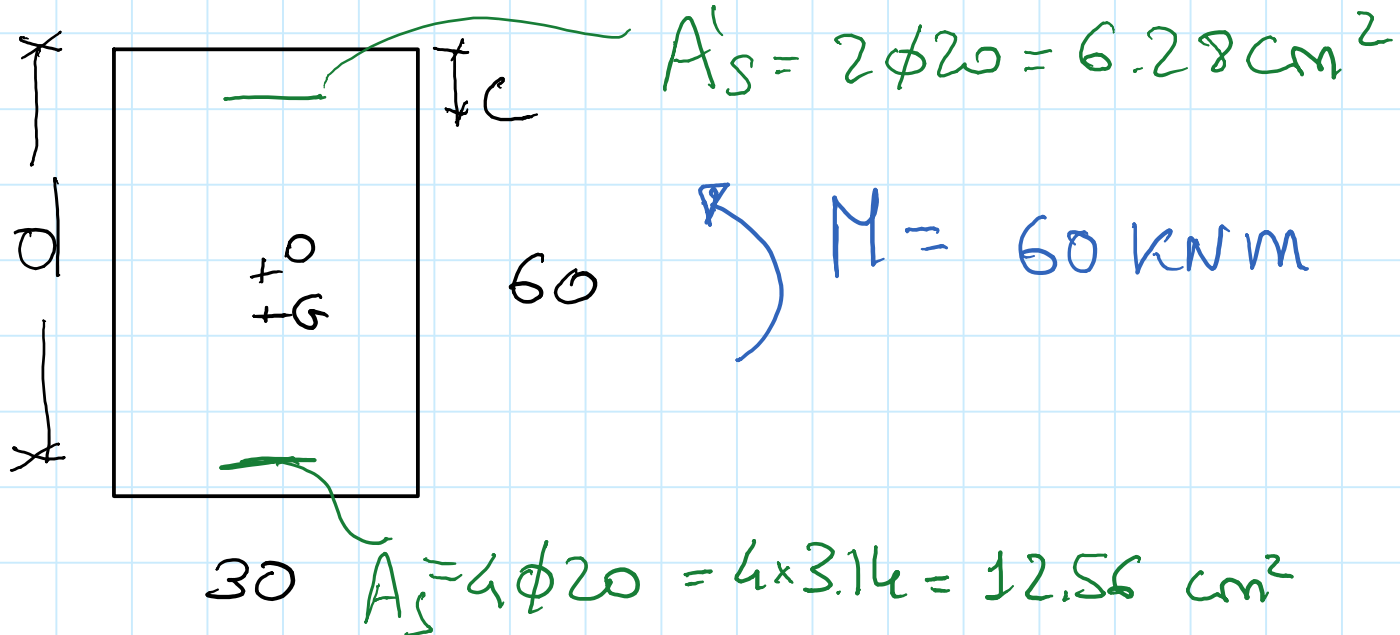
$$\sigma_t \leq f_{ctk}$$

$$\sigma_s' = -n \frac{M}{I_x} (dG,SUP - c)$$

$$\sigma_s = n \frac{M}{I_x} (dG,INF - c)$$

$$I_x = \frac{b dG,SUP^3}{3} + \frac{b dG,INF^3}{3} + n A's (dG,SUP - c)^2 + n A_s (dG,INF - c)^2$$

ESEMPIO: VERIFICA A FESSURAZIONE



C30/37 $\rightarrow \eta = 6.1$
B450 C
 $c = 5 \text{ cm}$
 $d = h - c = 55 \text{ cm}$

$$S_{sup} = \frac{30 \times 60^2}{2} + 6.1 \times 6.28 \times 5 + 6.1 \times 12.56 \times 55$$
$$= 58405.4 \text{ cm}^3$$

$$A = 30 \times 60 + 6.1 (6.28 + 12.56) = 1915 \text{ cm}^2$$

$$d_{G, sup} = \frac{58405.4}{1915} = 30.5 \text{ cm} ; d_{G, inf} = 29.5 \text{ cm}$$

$$I_x = \frac{30 \times 30,5^3}{3} + \frac{30 \times 29,5^3}{3} +$$

$$+ 6 \cdot 10 \times 6,28 \times (30,5 - 5)^2 + 6 \cdot 10 \times 12,56 (29,5 - 5)^2$$

$$= 611349 \text{ cm}^4$$

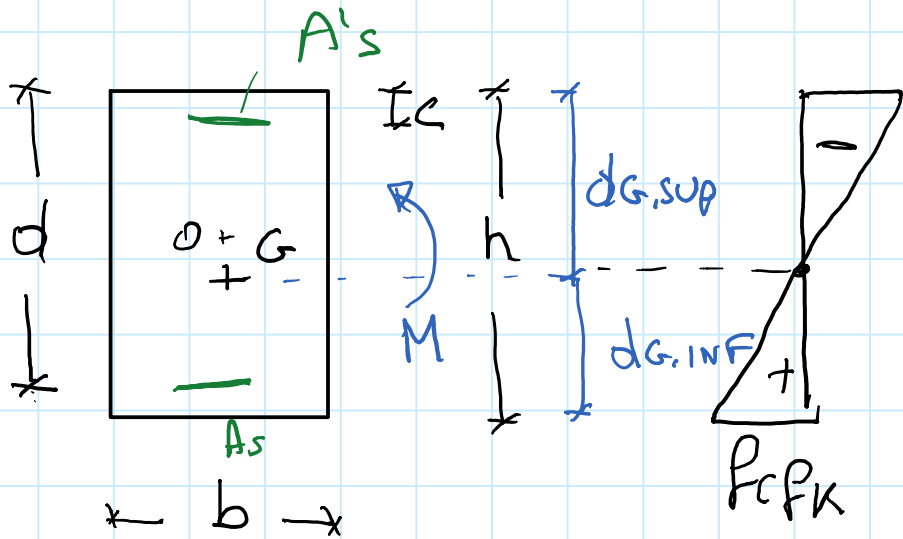
$$\sigma_{t,max} = \frac{M}{I_x} (d_{G,inf}) = \frac{60 \text{ kNm} \cdot 10^6 \times 29,5 \text{ cm}}{611349 \text{ cm}^4 \cdot 3 \cdot 10^3}$$

$$= 2,9 \text{ N/mm}^2$$

$$f_{ctk} = 1,2 f_{ctk} = 1,2 \times 2,02 \text{ MPa} = 2,4 \text{ MPa}$$

$\sigma_{t,max} > f_{ctk} \Rightarrow$ SEZIONE FESSURATA

MOMENTO DI FESSURAZIONE



$$\sigma_t = \frac{M}{I_x} d_{g,inf} = f_{ctk}$$

$$M_{fess} = f_{ctk} \cdot \frac{I_x}{d_{g,inf}}$$

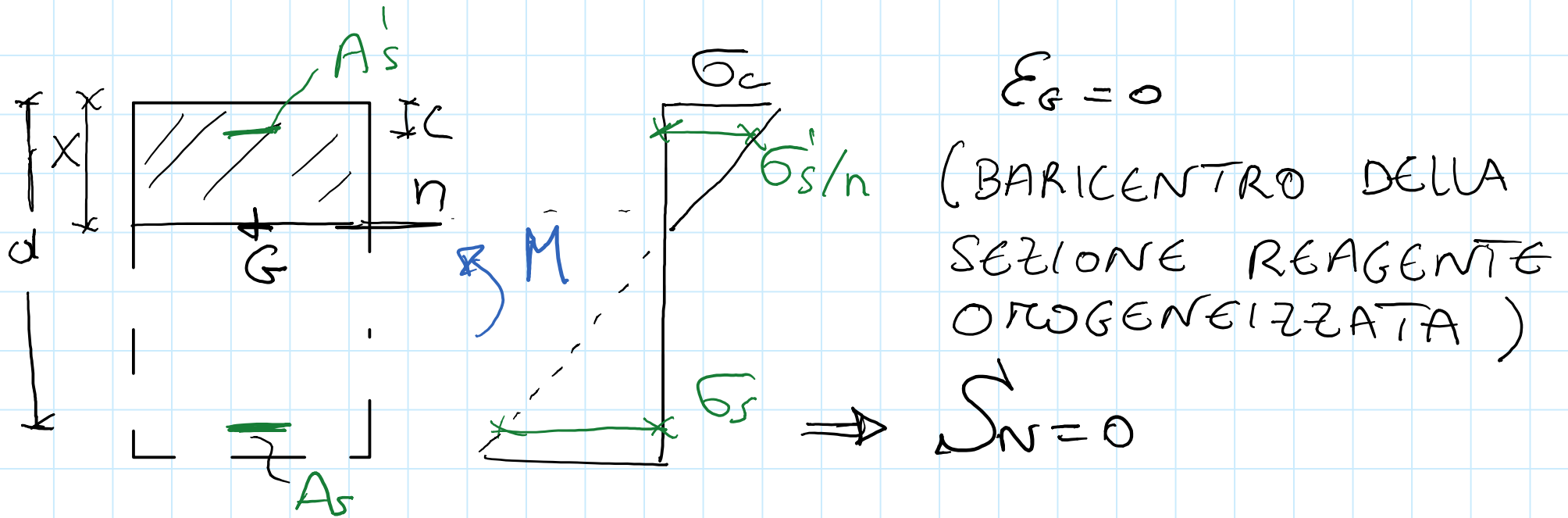
PER ESEMPIO PRECEDENTE

$$M_{fess} : f_{ctk} = M : \sigma_t \Rightarrow$$

$$M_{fess} : 2,4 \text{ MPa} = 60 \text{ kNm} : 2,9 \text{ MPa}$$

$$M_{fess} = \frac{60 \times 2,4}{2,9} = 49,7 \text{ kNm}$$

VERIFICA A FLESSIONE AL II STADIO



$$\sum N = -bx \cdot \frac{x}{2} - nA'_s(x-c) + nA_s(d-x) = 0$$

$$+ \frac{bx^2}{2} + xn(A'_s + A_s) - n(A'_sc + A_s d) = 0$$

$$x^2 + \frac{2n}{b}(A'_s + A_s)x - \frac{2n}{b}(A'_sc + A_s d) = 0$$

POSIZIONE ASSE NEUTRO

$$x^2 + \frac{2n}{b} (A'_s + A_s) x - \frac{2n}{b} (A'_s c + A_s d) = 0$$

$$x = -\frac{n}{b} (A'_s + A_s) \pm \sqrt{\frac{n^2}{b^2} (A'_s + A_s)^2 + \frac{2n}{b} (A'_s c + A_s d)}$$

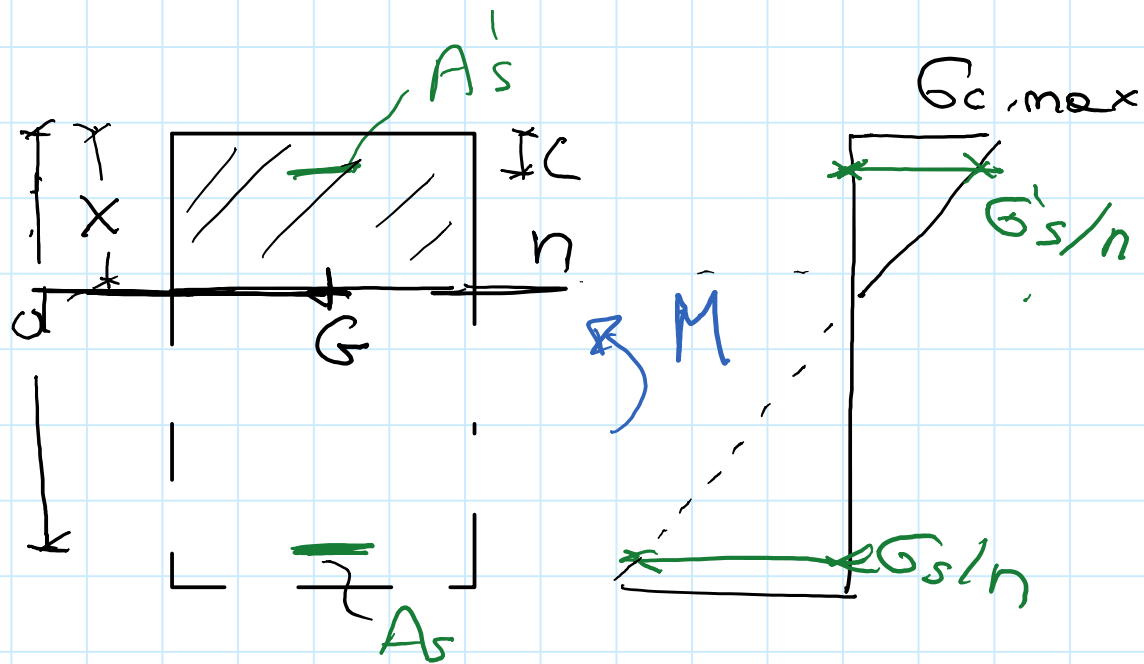
$$x = \underbrace{\frac{nd}{bd} (A'_s + A_s)}_{\psi d} \left[-1 + \sqrt{1 + \frac{2d}{bd} (A'_s c + A_s d) \cdot \frac{b^2 d}{dn^2 (A'_s + A_s)^2}} \right]$$

$$\psi = \text{PERC. ELASTICA DI ARMATURA} = n \frac{(A_s + A'_s)}{bd}$$

$$d_{gs} = \frac{A'_s c + A_s d}{A_s + A'_s} \quad \text{DISTANZA BARICENTRO ARMATURE DAL BORDO SUPERIORE}$$

$$x = \psi d \left[-1 + \sqrt{1 + \frac{2d_{gs}}{\psi d}} \right]$$

CALCOLO DELLE TENSIONI



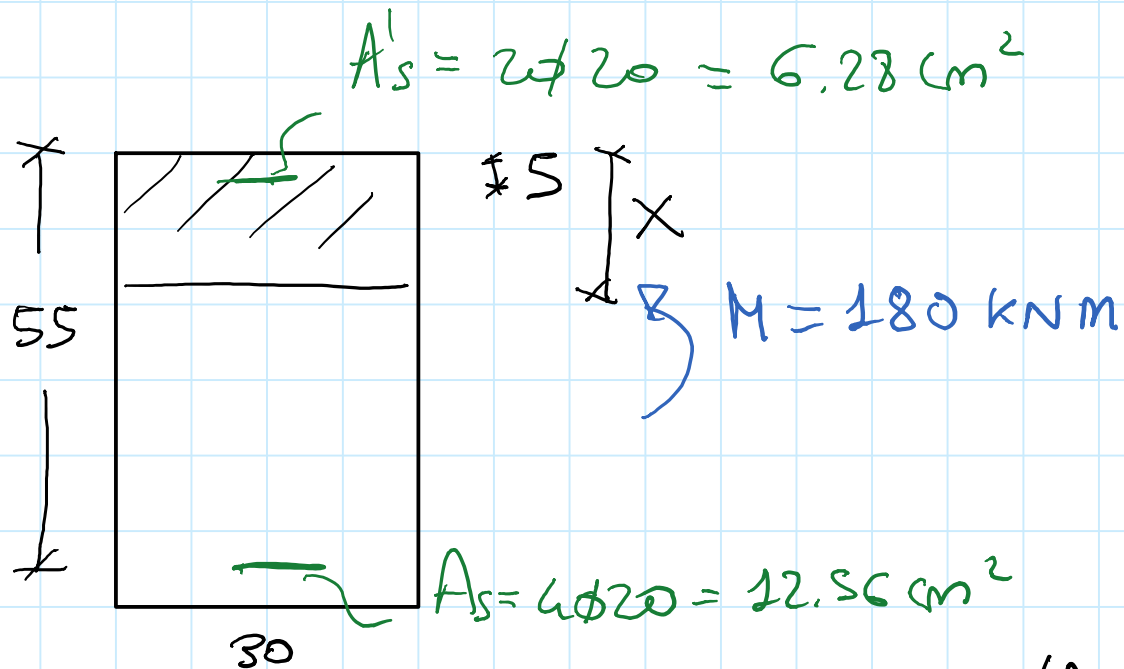
$$\sigma_{c,max} = -\frac{M}{I_x} x$$

RISPETTO ASSE // x
PASSANTE PER G

$$\sigma'_s = -n \frac{M}{I_x} (x - c) ; \quad \sigma_s = n \frac{M}{I_x} (d - x)$$

$$I_x = \frac{bx^3}{3} + nA'_s (x - c)^2 + nA_s (d - x)^2$$

ESEMPIO



30x60
C30/37 ; B450C

CARICHI DI LUNGA
DURATA

$$\sigma_c \leq 0.45 f_{ck}$$

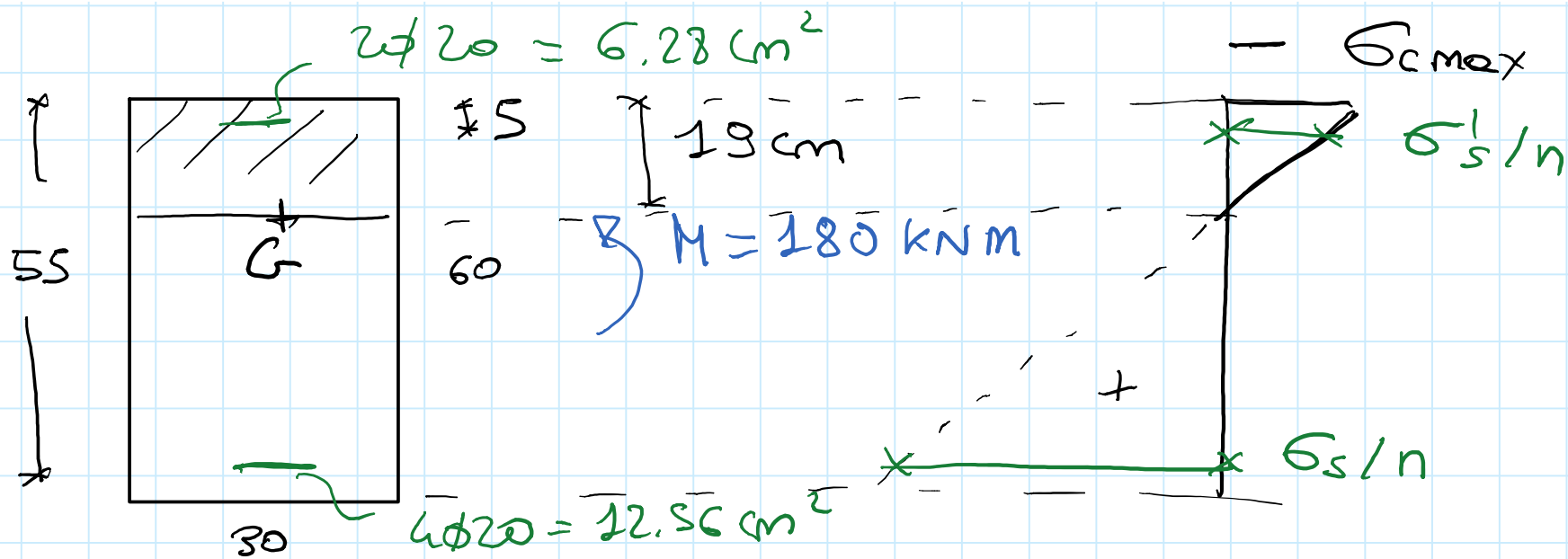
$$\sigma_s \leq 0.8 f_{yk}$$

PER TROVARE x

$$\eta = \frac{n(A_s + A'_s)}{bd} = \frac{15(12.56 + 6.28)}{30 \times 55} = 0.17$$

$$d_{G.SUP} = \frac{6.28 \times 5 + 12.56 \times 55}{6.28 + 12.56} = 38.3 \text{ cm}$$

$$x = 0.17 \cdot 55 \left[-1 + \sqrt{1 + \frac{2 \times 38.3}{0.17 \times 55}} \right] = 19 \text{ cm}$$



$$I_x = \frac{30 \times 19^3}{3} + 15 \times 6,28 \times (19 - 5)^2 + 15 \times 12,56 \times (55 - 19)^2 = 331219 \text{ cm}^4$$

$$\sigma_{cmax} = - \frac{180 \text{ kNm}}{331219 \text{ cm}^4} \cdot 19 \text{ cm} \times 10^3 = -10,33 \text{ MPa}$$

$$0,45 f_{ck} = 0,45 \times 30 \text{ N/mm}^2 = 13,5 \text{ MPa}$$

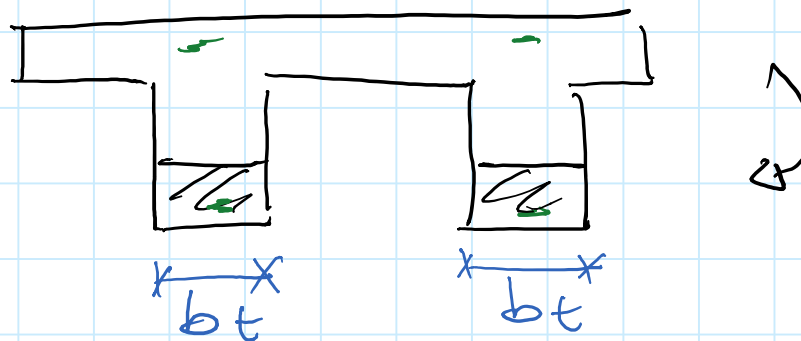
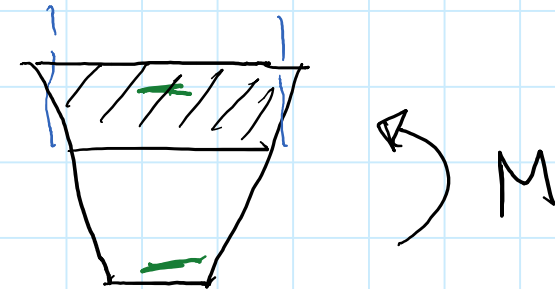
$$\sigma_s = 15 \times \frac{180 \text{ kNm}}{331219 \text{ cm}^4} \cdot (55 - 19) \text{ cm} \times 10^3 = 293,5 \text{ N/mm}^2$$

$$0,8 f_{yk} = 0,8 \times 450 \text{ N/mm}^2 = 360 \text{ N/mm}^2$$

SEZIONI RICONDUCEBILI AUA RETTANGOLARE

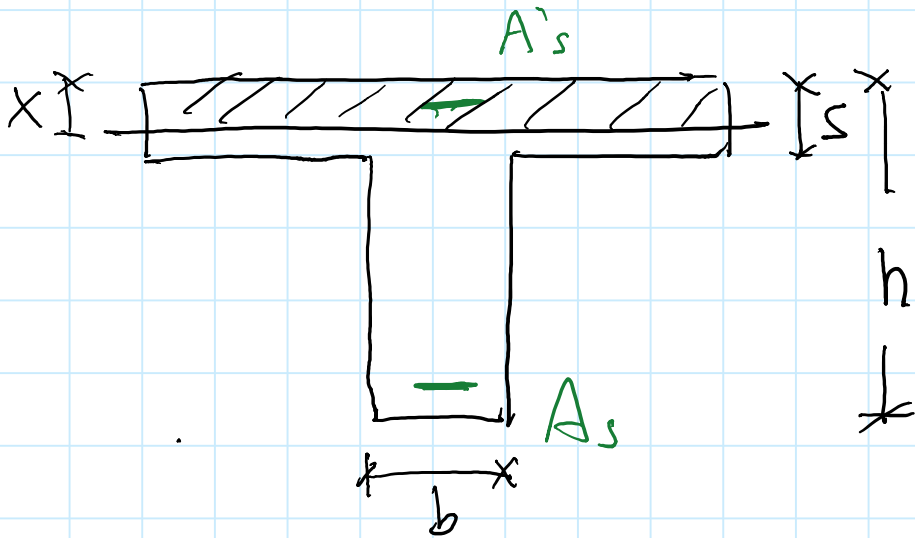


→ RIGOROSAMENTE
RETTANGOLARE



⇔ SEZ. RETTANGOLARE
 $b = 2bt$

SEZIONE A T

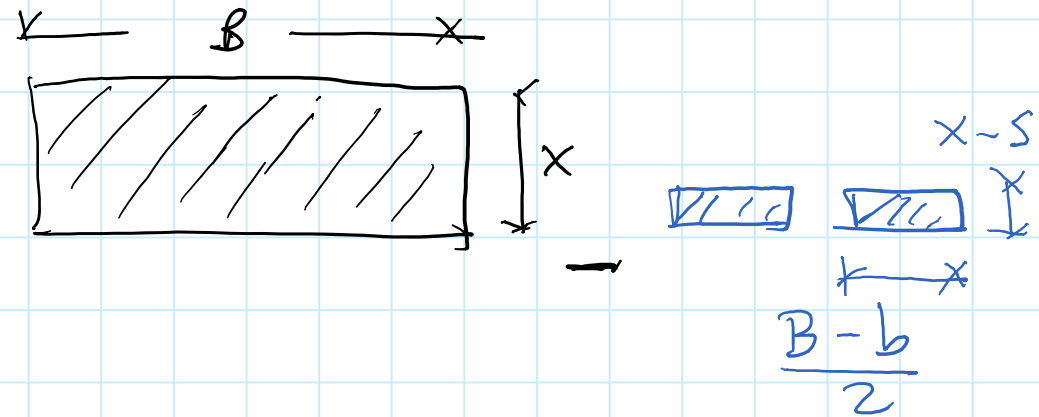
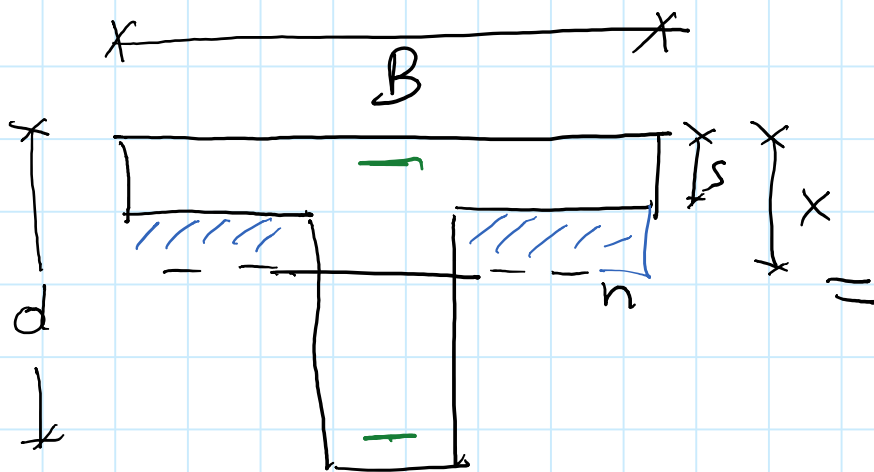


SUPPONGO $x \leq s$

⇒ APPLICO FORMULA
SEZ. RETTANGOLARE

$$x = \eta d \left[-1 + \sqrt{1 + \frac{2 \sigma_{cs}}{\eta d}} \right]$$

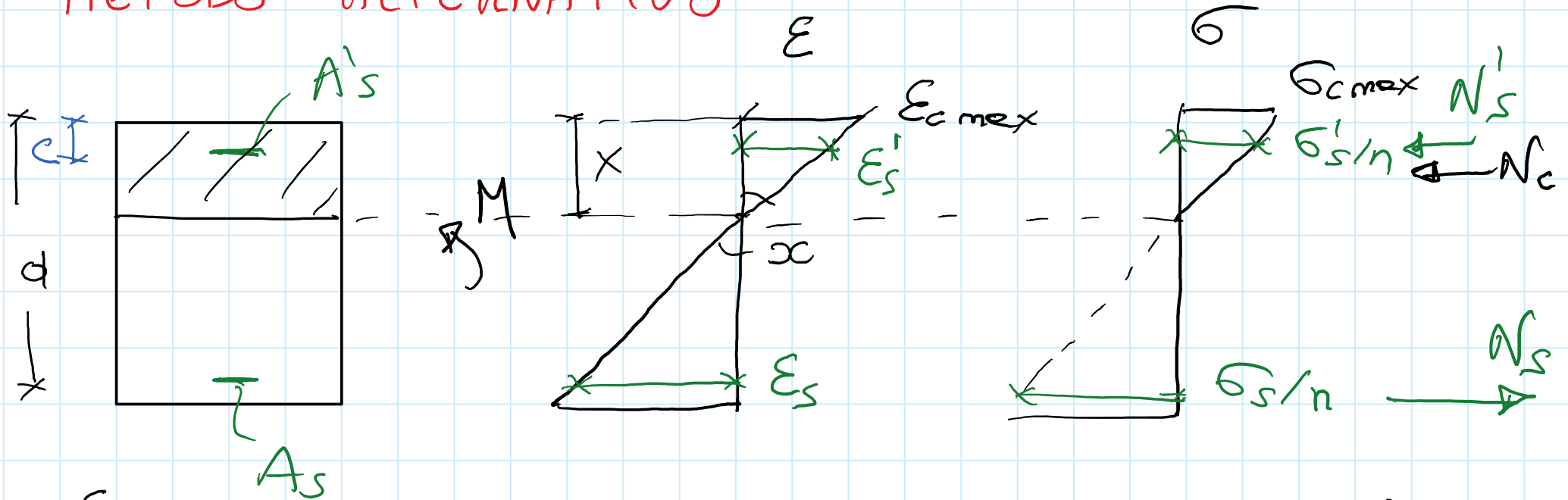
se $x > s$ ⇒ SEZIONE
A T



$$\sum N = 0$$

$$-Bx \cdot \frac{x}{2} + (B-b) \frac{(x-s)^2}{2} - nA'_s(x-c) + nA_s(d-x) = 0$$

METODO ALTERNATIVO



$$\epsilon_{cmox} = -\kappa X \rightarrow \sigma_{cmox} = E_c \epsilon_{cmox} = -\kappa X E_c$$

$$\epsilon'_s = -\kappa (x - c) \rightarrow \sigma'_s = E_s \epsilon'_s = -n E_c \kappa (x - c)$$

$$\epsilon_s = \kappa (d - x) \rightarrow \sigma_s = E_s \epsilon_s = n E_c \kappa (d - x)$$

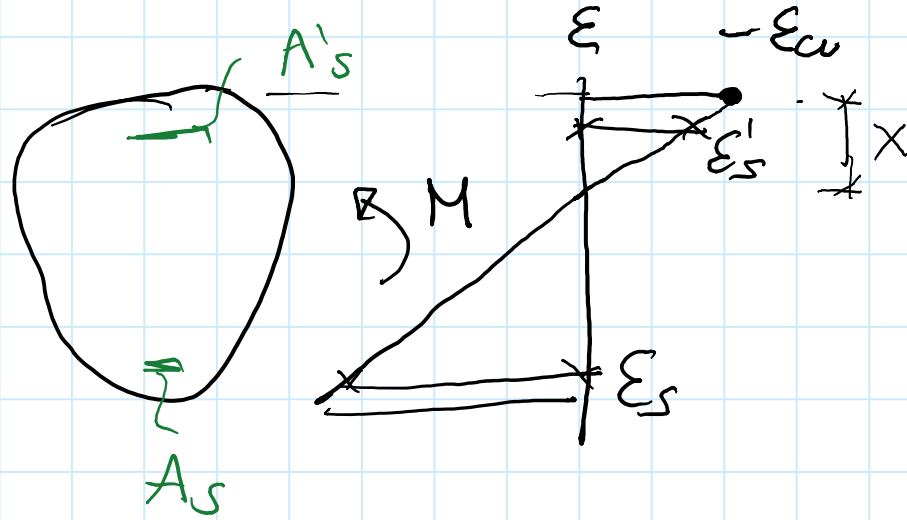
$$N_c = b x \cdot \frac{\sigma_{cmox}}{2} = -\kappa E_c b \frac{x^2}{2}$$

$$N_s = \sigma_s A_s = \kappa E_c \cdot n A_s (d - x)$$

$$N'_s = \sigma'_s A'_s = -\kappa E_c n A'_s (x - c)$$

$$N_c + N'_s + N_s = 0$$

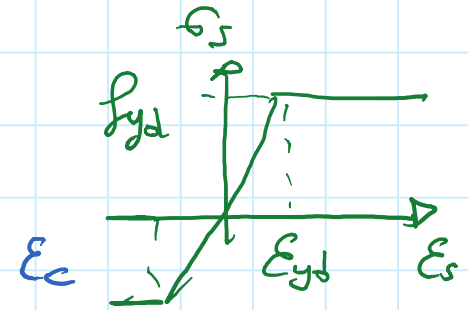
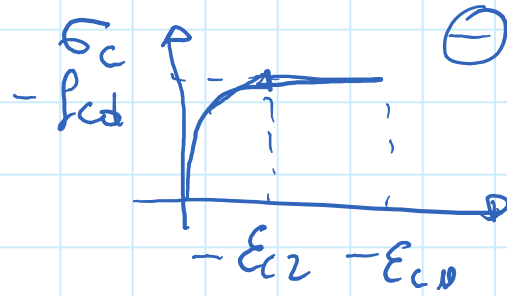
VERIFICA AL III STADIO (APPROCCIO GENERALE)



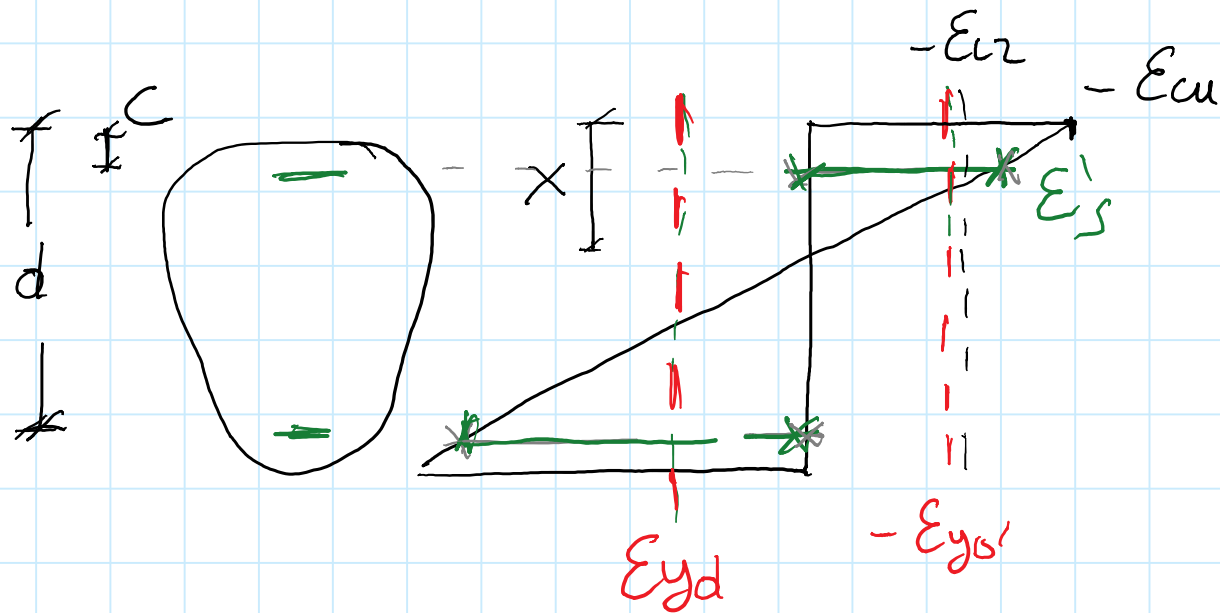
CALCOLARE

$$M_{red} \geq M_{ed}$$

1. FISSO DIAGR. ϵ LIMITE ($\epsilon = -\epsilon_{cu}$)
2. IPOTIZZO X
3. CALCOLO σ
4. CALCOLO N_c, N_s, N'_s
5. EQ. TRASLAZIONE $\rightarrow X$
6. EQ. ROTAZIONE $\rightarrow M_{red}$



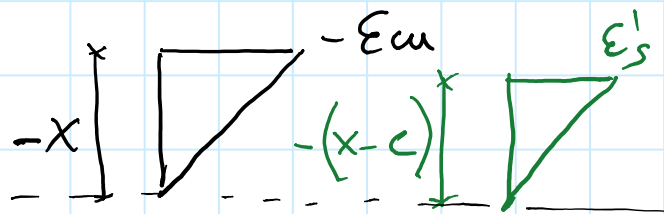
CALCOLO ϵ ARMATURE



$$\epsilon_{cu} = 3.5\text{‰}$$

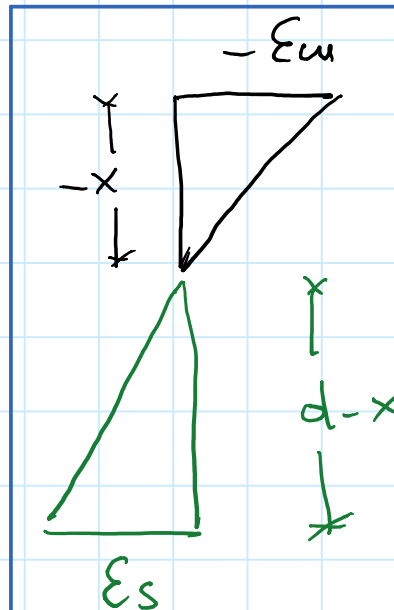
$$\epsilon_{c2} = 2.00\text{‰}$$

$$\epsilon_{yd} = \frac{f_{yd}}{E_s} = 1.96\text{‰}$$



$$-\epsilon_{cu} : (-x) = \epsilon'_s : [-(x-c)]$$

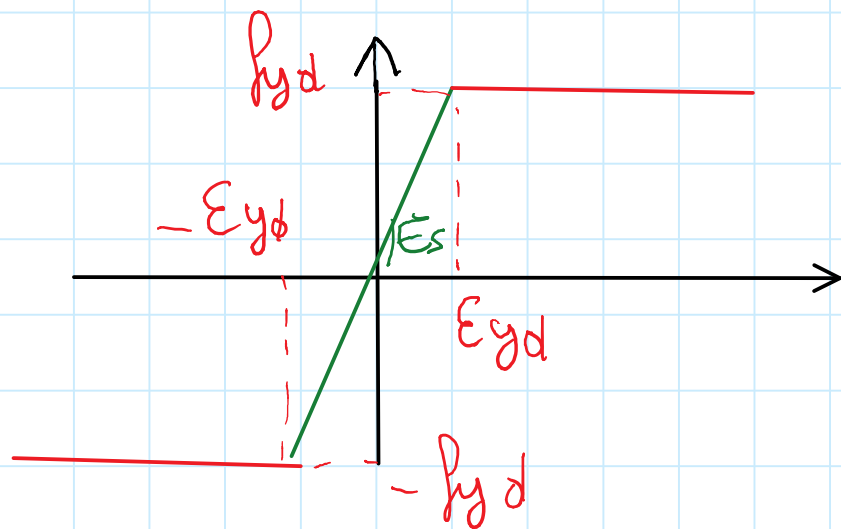
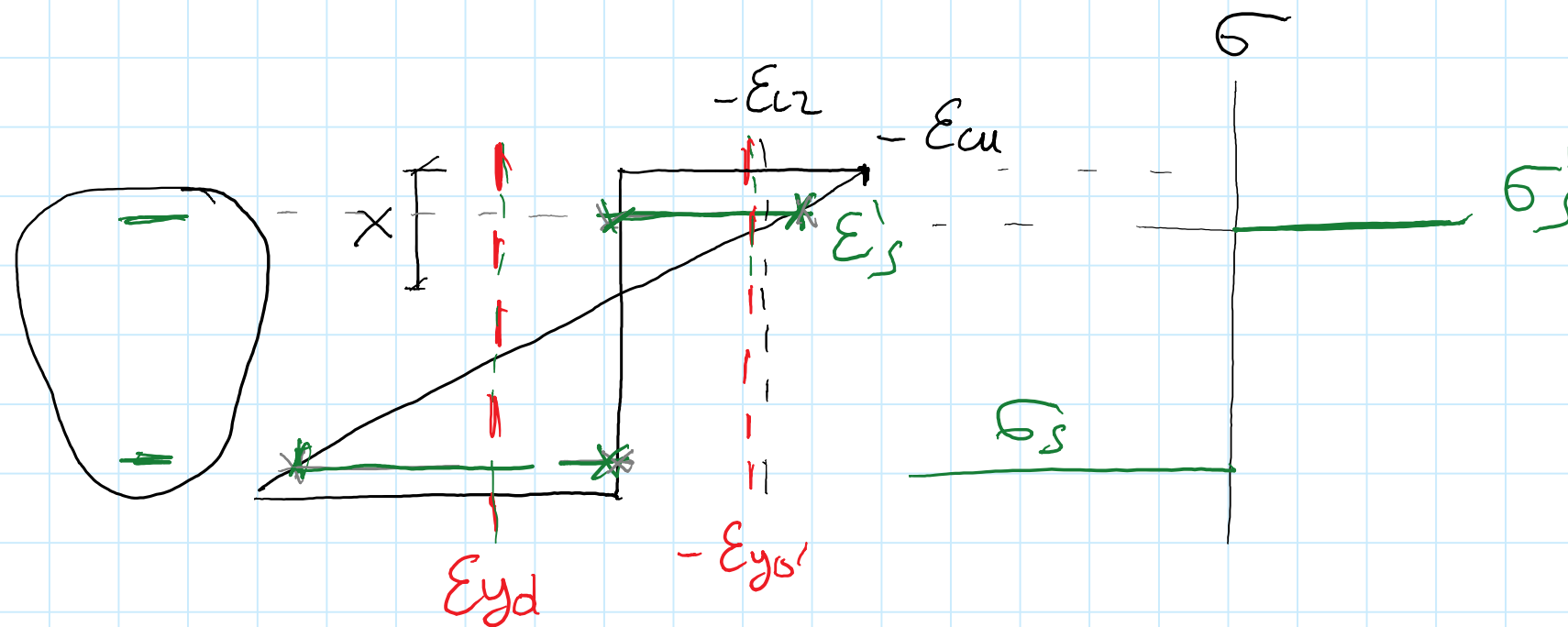
$$\epsilon'_s = -\frac{\epsilon_{cu}}{x} (x-c)$$



$$-\epsilon_{cu} : (-x) = \epsilon_s : (d-x)$$

$$\epsilon_s = \frac{\epsilon_{cu}}{x} (d-x)$$

TENSIONI NELL'ARMATURA

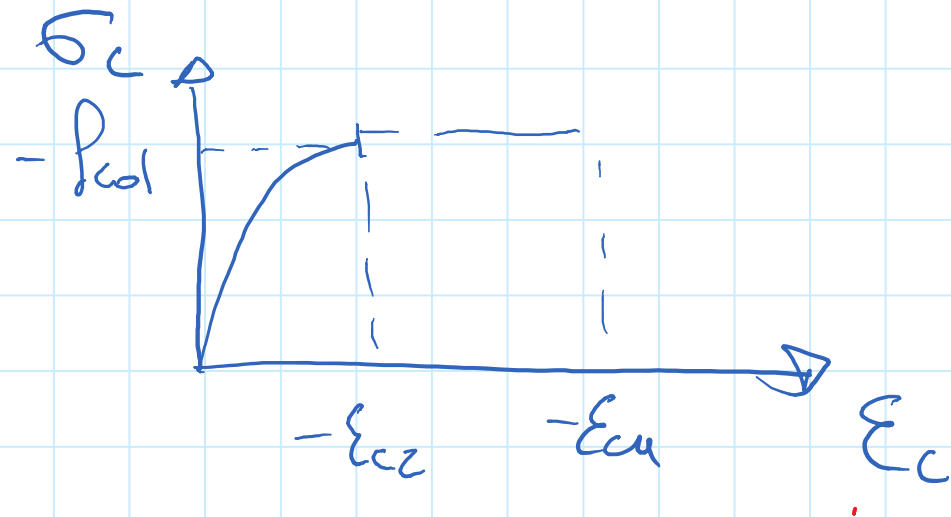
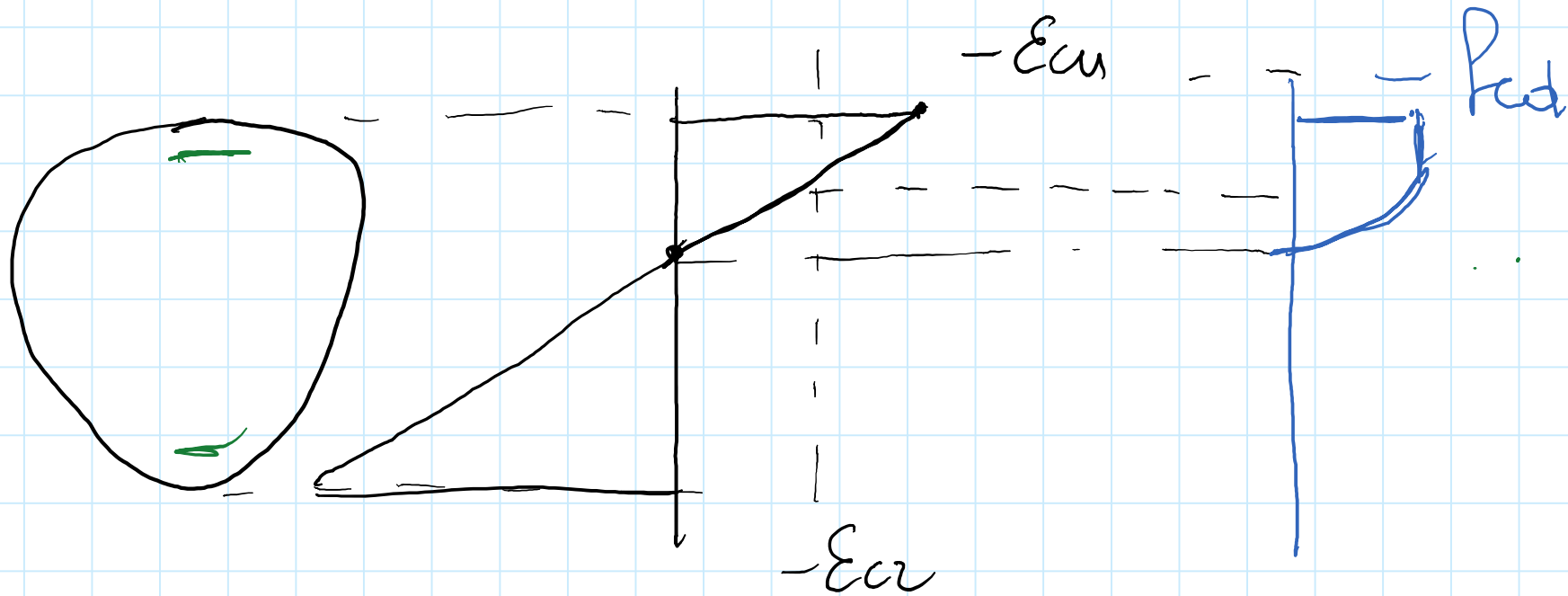


se $\epsilon_s \geq \epsilon_{yd} \rightarrow \sigma_s = f_{yd}$

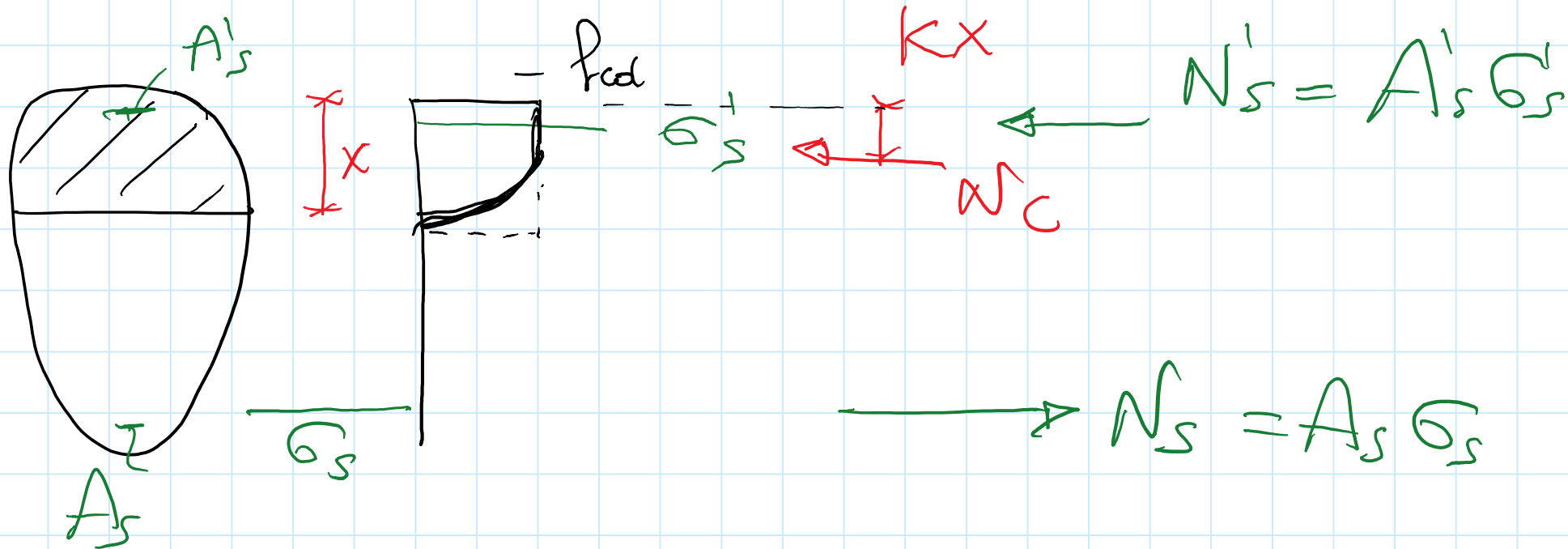
se $-\epsilon_{yd} < \epsilon_s < \epsilon_{yd} \rightarrow \sigma_s = E_s \epsilon_s$

se $\epsilon_s < -\epsilon_{yd} \rightarrow \sigma_s = -f_{yd}$

TENSIONI NEL CALCESTRUZZO



CALCOLO RESULTANTI



$$N_c = \int_{A_c} \sigma dA = \beta f_{cd} A_c$$

$\beta = \text{COEFF. DI RIEMPIMENTO} = \frac{\int \sigma dA_c}{f_{cd} A_c}$
 $K = \text{COEFF. DI PROFONDITA'}$